Compact analytic groups over pro-p domains of positive characteristic

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Abstract

While the theory of Lie groups is highly developed in characteristic 0, comparatively little is known about analytic groups over local fields of positive characteristic p. More generally, one can consider groups which are analytic over pro-pdomains R, without restricting the Krull dimension to 1. Natural examples of such rings are power series rings over finite fields, e.g. $R = F_p[t_1, \ldots, t_m]$.

In my talk I will address open problems regarding compact R-analytic groups where R is a pro-p domain of characteristic p. I will report on several structural results which hold in the special case where R has Krull dimension 1. The talk will be based on a joined paper with Andrei Jaikin-Zapirain [J. London Math. Soc. **76** (2007), 365–383].